Current Comments

The 200 "Pure" Mathematicians Most Cited in 1978 and 1979, Including a List of Most-Cited Publications for the Top 100

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In our study of the 1,000 most-cited scientists publishing from 1965 to 1978, there were no mathematicians listed. In an earlier study of the 250 most-cited authors in *Science Citation Index*® (*SCI*®) from 1961 to 1975, only 13 were not in the life or physical sciences. Almost all of these were statisticians—not pure mathematicians.

There are many reasons why mathematicians are "underrepresented" on these lists. These include the size of the math literature and the related fact that the average math paper contains fewer references than papers in the life and physical sciences. For example, the average biochemistry paper contains three times as many references as the average math paper.³

One does not need to perform citation analyses to confirm the truism that mathematicians make important contributions to the advance of science. And the literature of mathematics is now quite large. In recognition of this fact, we've launched a new data base covering pure and applied mathematics called ISI/CompuMathTM. 4 To cover this literature efficiently, we identified the most important pure and applied math journals.3 Much earlier, we identified the most-cited papers and books in mathematics, 5,6 But this is the first time we've done a separate study of the mostcited math authors.

We relied on the math journals listed in SCI in 1979 to identify the mathematicians most cited by current mathematicians. Specifically, we examined those 71 journals listed under the "mathematics" subject category in the SCI Guide and List of Source Publications. We excluded multidisciplinary journals, such as Doklady Akademii Nauk SSSR and Comptes Rendus Hebdomadaires des Séances de l'Académie des Sciences Series A, that also publish large sections on physics and astronomy, for example. We were left with a list of 64 "pure" math journals, shown in Table 1.

All references appearing in the 1978 and 1979 volumes of these journals were processed. The cited authors were ranked by frequency of combined citations in those two years. The list of cited authors was then examined for homographs-two or more individuals with the same surname and initials. Finally, we looked up citations they received from all journals indexed in SCI. This added citations from physicists, astronomers, theoretical biologists, and other scientists publishing in the journals from those fields. Table 2 shows the 100 mostcited mathematicians in 1978 and 1979 in alphabetical order. Also shown are their institutional affiliations and the number of citations from both the "core" pure math journals and all SCI journals.

While this method for identifying highly cited pure mathematicians in our data base isn't perfect, it seemed the best approach. For example, the distinguished French mathematician René Thom does not appear in Table 2. In 1978 and 1979, Thom's publications

Table 1: Math journals indexed in the 1979 SCI® used to identify the top 100 most-cited mathematicians, 1978 and 1979.

Acta Mathematica Academiae Scientiarum Hungaricae

Acta Mathematica—Djursholm

Advances in Mathematics

American Journal of Mathematics

American Mathematical Monthly Annals of Mathematics

Annais of Mathematics Archiv der Mathematik

Arkiv for Matematik

Bulletin de la Societe Mathematique de France Bulletin of the American Mathematical Society

Canadian Journal of Mathematics

Commentarii Mathematici Helvetici

Communications in Algebra

Compositio Mathematica

Discrete Mathematics

Duke Mathematical Journal

Fibonacci Quarterly

Illinois Journal of Mathematics

Indiana University Mathematics Journal

Inventiones Mathematicae

Israel Journal of Mathematics

Journal d'Analyse Mathematique

Journal fur die Reine und Angewandte Mathematik

Journal of Algebra

Journal of Approximation Theory

Journal of Combinatorial Theory Series A

Journal of Combinatorial Theory Series B

Journal of Differential Equations

Journal of Functional Analysis

Journal of Graph Theory

Journal of Mathematical Analysis and Applications

Journal of Number Theory

Journal of the London Mathematical Society-

Second Series

Journal of the Mathematical Society of Japan

Manuscripta Mathematica

Mathematica Scandinavica Mathematical Notes

Mathematical Proceedings of the Cambridge Philosophical

Society

Mathematics of the USSR-Izvestiia

Mathematics of the USSR-Sbornik

Mathematika

Mathematische Annalen

Mathematische Nachrichten

Mathematische Zeitschrift Memoirs of the American Mathematical Society

Michigan Mathematical Journal

Monatshefte fur Mathematik

Nagoya Mathematical Journal

Pacific Journal of Mathematics
Proceedings of the American Mathematical Society

Proceedings of the Edinburgh Mathematical Society

Proceedings of the Indian Academy of Sciences-

Mathematical Sciences

Proceedings of the Japan Academy Series A-

Mathematical Sciences

Proceedings of the Koninklijke Nederlandse Akademie van Wetenschappen Series A—Mathematical Sciences Proceedings of the London Mathematical Society

Proceedings of the Royal Society of Edinburgh

Section A-Mathematics

Quarterly Journal of Mathematics

Ricerche di Matematica

Semigroup Forum

Siberian Mathematical Journal

Studia Mathematica

Transactions of the American Mathematical Society

Topology

Zeitschrift fur Mathematische Logik und Grundlagen

der Mathematik

were cited 404 times, but only 62 of these citations were from pure math journals. Non-journal items—books, proceedings, series, etc.—accounted for 264. Similarly, Andrey Kolmogorov also does not appear on our list, although he has been described as "the 20th century's most influential Soviet mathematician." Kolmogorov's publications were cited 525 times in 1978 and 1979. However, just 69 of these were from the pure math journals in Table 1.

Several mathematicians we consulted commented that many other "significant" people do not appear on the list. When we extended the study to include 200 authors, almost all of the mathematicians mentioned were included. For example, Kolmogorov is included in Table 3, which lists the next 100 mathematicians who were most cited in 1978-1979. (There are actually 103 names in Table 3 because of a tie.) But we are limited by time and space to study only the top 100 most-cited mathematicians in detail. Of course, there still might be some mathematicians perceived as significant who were not highly cited during the two vears studied.

Ten authors listed in Table 2 have received the Fields Medal: L.V. Ahlfors. 1936; L. Schwartz, 1950; J.P. Serre, 1954; L.V. Hormander and J.W. Milnor, 1962; M.F. Atiyah and A. Grothendieck, 1966; D.B. Mumford, 1974; and P. Deligne and D.G. Quillen, 1978. Five more Fields Medalists appear in Table 3: K. Kodaira, 1954; S. Smale, 1966; H. Hironaka and J.G. Thompson, 1970; and C.L. Fefferman, 1978. The Fields Medal is awarded every four years by the International Mathematical Union to young mathematicians for their outstanding achievements. John Charles Fields, former mathematics professor at the University of Toronto, set up a trust fund for the medal in his will. The medal was described in Science as "an award comparable in many respects to the Nobel Prize in the prestige it confers."8 The Table 2: The top 100 mathematicians most cited in 1978 and 1979. Asterisks indicate Fields Medal winners. A = citations from the math core journals in 1978 and 1979. B = total citations from SCI^* journals in 1978 and 1979.

		ie main core journais in 1978			= lotal citations from 3C7 jo			7/0 and 19/9.
	B	Adams John Produ	102	B	Course Blokand	A.	B	U C U
164	202	Adams, John Frank	103	650		284	461	Hardy, Godfrey Harold
		University of Manchester			New York University			University of Cambridge
		Manchester, UK	. 20		New York, NY		217	Cambridge, UK
164	265	Agmon, Shravel	128	159	Curtis, Charles Whittlesey	161	217	Harish-Chandra
		Hebrew University			University of Oregon			Institute for Advanced Study
		Jerusalem, Israel			Eugene, OR			Princeton, NJ
117	171	*Ahlfors, Lars Valerian	145	170	Deligne, Pierre	138	235	Hartman, Philly
		Harvard University			Institut des Hautes Etudes			Johns Hopkins University
		Cambridge, MA			Scientifiques			Baltimore, MD
108	127	Alisen, Erik Magnus			Bures-sur-Yvette, France	141	162	Hartshorne, Robert Cope
		University of Oslo	148	263	Dieudonne, Jean Alexandre			University of California
		Oslo, Norway			University of Nice			Berkeley, CA
140	157	Artin, Michael			Nice, France	125	138	
		Massachusetts Institute of	346	435	Dixmier, Jacques			University of Hamburg
		Technology			University of Paris VI			Hamburg, FRG
		Cambridge, MA			Paris, France	155	237	Helgason, Sigurdur
166	166	Aschbacher, Michael	111	137	Douglas, Ronald George			Massachusetts Institute of
		California Institute of			State University of			Technology
		Technology			New York			Cambridge, MA
		Pasadena, CA			Stony Brook, NY	139	157	Herstein, Israel N.
252	444	'Atiyah, Michael Francis	324	514	Dunford, Nelson			University of Chicago
		Oxford University			Yale University			Chicago, IL
		Oxford, UK			New Haven, CT	193	257	Hewitt, Edwin
126	136	Auslander, Maurice	101	824	Erdelyl, Arthur			University of Washington
		Brandeis University			University of Edinburgh			Seattle, WA
		Waltham, MA			Edinburgh, UK	154	309	Hille, Einer
222	255		295	485	Erdos, Paul			University of California
		Columbia University			Hungarian Academy of			La Jolla, CA
		New York, NY			Sciences	119	167	Hilton, Peter John
110	718				Budapest, Hungary			Case Western Reserve
		University of Southern	119	125				University
		California			Yale University			Cleveland, OH
		Los Angeles, CA			New Haven, CT	115	152	
131	333		161	356	Friedman, Avner			University of Bonn
101	,,,,,	CNRS	101	3.00	Northwestern University			Bonn. FRG
		Paris, France				114	401	*Hormander, Lars
129	116	Birkhoff, Garrett		220	Evanston, IL	,1,74	471	
129	338	·	177	220	Fuchs, Laszlo			Volter
		Harvard University			Tulane University			University of Lund
207	24.7	Cambridge, MA	205	=	New Orleans, LA			Lund, Sweden
297	387	Borel, Armand	207	748	Geliand, Izrail	178	189	Huppert, Bertram
		Institute for Advanced			Moiseevich			University of Mainz
		Study			Mathematics Institute			Mainz, FRG
		Princeton, NJ			USSR Academy of Sciences	111	123	lwasawa, Kenkichi
517	723				Moscow, USSR			Princeton Univ.
		France	109	112	Glauberman, George Isaac			Princeton, NJ
137	167	Brauer, Richard Dagobert			University of Chicago	261	343	Jacobson, Nathan
		Harvard University			Chicago, IL			Yale University
		Cambridge, MA	103	269	Gokhberg, Israel			New Haven, CT
115	120				TSudíkovích	225	285	
		Rutgers University			Tel Aviv University			University of Chicago
		New Brunswick, NJ			Tel Aviv, Israel			Chicago, IL
173	342	Brezis, Haim	293	321	Gorenstein, Daniel	131	638	Karlin, Samuel
		University of Paris VI			Rutgers University			Stanford University
		Paris, France			New Brunswick, NJ			Stanford, CA
190	250	Browder, Felix Earl	126	131		247		
		University of Chicago			University of Gottingen	343	646	Kato, Toslo
		Chicago, IL			Gottingen, FRG			University of California
101	140	Calderon, Alberto Pedro	479	560	'Grothendleck, Alexandre		•	Berkeley, CA
		University of Chicago			University of Montpellier II	144	201	Kobayashi, Shoshichi
		Chicago, IL			Montpellier, France			University of California
179	207	Carlitz, Leonard	106	369	Hale, Jack Kenneth			Berkeley, CA
		Duke University			Brown University	131	263	Krasnoselskii, Mark
		Durham, NC			Providence, RI			Aleksandrovich
167	236	Carian, Henri Paul	147	199	Hall, Marshall			Moscow Control Problems
		University of Paris XI			California Institute of			Institute
		Paris, France			Technology			Moscow, USSR
121	178				Pasadena. CA	136	212	Kuratowski, Kazimierz
131	1/6		207	492				Warsaw University
		Hoblitzelle Tulane University	207	472				Warsaw, Poland
					Indiana University	124	285	Ladyzhenskaia, Olga
,	, .~	New Orleans, LA	201	40.7	Bloomington, IN			Aleksandrovna
112	147		201	483				Leningrad University
		University of London			University of Michigan			Leningrad, USSR
		London, UK			Ann Arbor, MI			<u>.</u>

A	В		A	В		A	В	
227	311	Lang, Serge	113	269	Polys, George	102	126	Spanier, Edwin Henry
		Yale University			Stanford University			University of California
		New Haven, CT			Stanford, CA			Berkeley, CA
108	404	Lax, Peter David	137	164	'Quillen, Daniel G.	253	394	
		New York University			Massachusetts Institute of			Princeton University
		New York, NY			Technology			Princeton, NJ
150	167	Lindenstrauss, Joram			Cambridge, MA	104	112	Swan, Richard Gordon
		Hebrew University	109	370	Rockafellar, Ralph Tyrrell			University of Chicago
		Jerusalem, Israel			University of Washington			Chicago, IL
210	552	Lions, Jacques-Louis			Seattle, WA	137	339	Titchmarsh, Edward Charles
		College de France	224	349	Rudin, Walter			Oxford University
		Paris, France			University of Wisconsin			Oxford, UK
112	140	Lorentz, George G.			Madison, WI	104	190	Tutte, William Thomas
		University of Texas	110	138	Sakai, Shoichiro			University of Waterloo
		Austin, TX			Nihon University			Waterloo, Canada
137	249	Mackey, George			Tokyo, Japan	145	162	Wall, Charles Terence
		Whitelaw	111	153	Sato, Mikio			Clegg
		Harvard University			Kyoto University			University of Liverpool
		Cambridge, MA			Kyoto, Japan			Liverpool, UK
125	188	MacLane, Saunders	133	172	Schaefer, Helmut H.	187	248	Well, Andre
		University of Chicago			University of Tubingen			Institute for Advanced Study
		Chicago, IL			Tubingen, FRG			Princeton, NJ
105	133	May, J. Peter	125	325	'Schwartz, Laurent	110	487	Weyl, Hermann
		University of Chicago			Ecole Polytechnique			Institute for Advanced Study
		Chicago, 1L			Plaiseau, France			Princeton, NJ
415	542	'Milnor, John Willard	390	463	Serre, Jean-Pierre	131	190	
		Institute for Advanced Study			College de France			Institute for Advanced Study
		Princeton, NJ			Paris, France			Princeton, NJ
206	228	'Mumford, David Bryant	160	185	Shimura, Goro	190	214	Zariski, Oscar
		Harvard University			Princeton University			Harvard University
		Cambridge, MA			Princeton, NJ			Cambridge, MA
119	147		129	196	Siegel, Carl Ludwig	213	290	Zygmund, Antoni
		Kyoto University			University of Gottingen			University of Chicago
		Kyoto, Japan			Gottingen, FRG			Chicago, IL

Table 3: The next 103 mathematicians most cited in 1978 and 1979. Asterisks indicate Fields Medal winners. A = citations from the math core journals in 1978 and 1979. B= total citations from SCP journals in 1978 and 1979.

A	В		A	В		A	В	
70	90	Amann, Herbert	77	91	Bousfield, Aldridge Knight	74	162	Crandall, Michael G.
		University of Zurich			University of Illinois			University of Wisconsin
		Zurich, Switzerland			Chicago, IL			Madison, WI
8	76	Amitsur, Shimshon A.	83	109	Bowen, Robert E.	87	91	Day, Mahlon M.
		Hebrew University			University of California			University of Illinois
		Jerusalem, Israel			Berkeley, CA			Urbana, IL
1	80	Andreotti, Aldo	89	95	Browder, William	69	89	Demazure, Michael
		University of Strasbourg			Princeton University			Ecole Polytechnique
		Strasbourg, France			Princeton, NJ			Plaiseau, France
1	387	Arnold, Victor Igorevich	69	76	Carleson, Lennart Axel	91	109	Dickson, Leonard E.
		University of Moscow			Edvard			University of Chicago
		Moscow, USSR			Mittag-Leffler Institute			Chicago, IL
4	123	Artin, Emil			Djursholm, Sweden	70	92	Diestel, Joseph
		University of Hamburg	100	111	Cassels, John William Scott			Kent State University
		Hamburg, FRG			University of Cambridge			Kent, OH
4	98	Arveson, William Barnes			Cambridge, UK	69	90	Dold, Albrecht
		University of California	87	142	Chern, Shiing-Shen			University of Heidelberg
		Berkeley, CA			University of California			Heidelberg, FRG
3	90	Auslander, Louis			Berkeley, CA	100	171	Effenberg, Samuel
		City University of New York	93	133	Chevalley, Claude			Columbia University
		New York, NY			University of Paris VIII			New York, NY
9	154	Bers, Lipman			Paris, France	81	93	Everitt. William Norrie
		Columbia University	76	194	Coddington, Earl A.			University of Dundee
		New York, NY			University of California			Dundee, UK
3	104	Bing, R.H.			Los Angeles, CA	74	104	Federer, Herbert
		University of Texas	78	87	Conner, Pierre Euclide			Brown University
		Austin, TX			Louisiana State University			Providence, R1
2	105	Boas, Ralph P.			Baton Rouge, LA	100	121	'Fefferman, Charles Louis
		Northwestern University	83	113	Connes, Alain			Princeton University
		Evanston, IL			Institut des Hautes Etudes			Princeton, NJ
3	100	Bonsall, Frank Featherstone			Scientifiques	91	885	Feller, William
-		University of Edinburgh			Bures-sur-Yvette, France			Princeton University
		Edinburgh, UK	78	119	Coxeter, Harold Scott			Princeton, NJ
9	118	Bott, Raoul	,,,	•••	MacDonald	70	76	Fox, Ralph H.
	- • •	Harvard University			University of Toronto			Princeton University

	_			D			ь	
A 86	B 97	Frohlich, Albrecht	A.	B 118	Kothe, Gottfried	A 97	В 271	Segal, Irving Ezra
00	7.	University of London	73	116	University of Frankfurt	7.	4/1	Massachusetts Institute of
		London, UK			Frankfurt, FRG			Technology
73	91	Gabriel, Pierre	92	130				Cambridge, MA
		University of Zurich			Institute of Physical	81	QR	Sierpinski, Waciaw F.
		Zurich, Switzerland			Chemistry	01	,0	Warsaw University
75	90	Gamelin, Theodore W.			Odessa, USSR			Warsaw, Poland
		University of California	82	88	Lambek, Joachim	00	207	,
		Los Angeles, CA			McGill University	99	287	Simon, Barry Martin
80	103	Gillman, Leonard	70	150	Montreal, Canada			California Institute of Technology
		University of Texas	78	98	Luxemburg, Wilhelmus			Pasadena, CA
78	79	Austin, TX Goldschmidt, David M.			Anthonius Josephus California Institute of			
7.0		University of California			Technology	98	225	Smale, Stephen
		Berkeley, CA			Pasadena, CA			University of California
68	97		99	259	Magnus, Wilhelm			Berkeley, CA
		University of Manitoba			Polytechnic Institute of	72	77	•
		Winnipeg, Canada			New York			University of California
94	109				New York, NY			Berkeley, CA
		Harvard University	92	135	Michael, Ernest Arthur	82	146	
97		Cambridge, MA			University of Washington			Princeton University
97	115	Gunning, Robert Clifford Princeton University	85	102	Scattle, WA Moore, Calvin C.	70	70	Princeton, NJ
		Princeton, NJ	0.3	102	University of California	70	70	•
94	117	Hall, Philip			Berkeley, CA			University of California Los Angeles, CA
		University of Cambridge	78	90		0.7		-
		Cambridge, UK			University of California	87	106	
69	73	Hayman, Walter Kurt			Berkeley, CA			Institut des Hautes Etudes Scientifiques
		University of London	89	294	Neumann, John Von			Bures-sur-Yvette, France
		London, UK			Institute for Advanced Study			
82	88	Higman, Graham			Princeton, NJ	73	73	
		Oxford University	72	113				University of Illinois Urbana, IL
94		Oxford, UK			Steklov Institute of	73	222	
74	112	*Hironaka, Helsuke Harvard University			Mathematics	7.2	232	Szego, Gabor Stanford University
		Cambridge, MA			Moscow, USSR			Stanford, CA
76	143	Hirsch, Morris William	68	85	,	02	172	
		University of California			Rutgers University	72	1/2	Szokefalvi-Nagy, Bela University of Szeged
		Berkeley, CA	7.	124	New Brunswick, NJ			Szeged, Hungary
87	119	Hochschild, Gerhard P.	/-4	124	Palais, Richard Sheldon Brandeis University	RR.	127	
		University of California			Waltham, MA	(10)	127	University of California
	20	Berkeley, CA	74	82	Pederson, Gert Kjaergard			Los Angeles, CA
81	90	Hochster, Melvin			University of Copenhagen	95	101	Tate, John T.
		University of Michigan Ann Arbor, MI			Copenhagen, Denmark			Harvard University
81	118	Holiman, Kenzeth	8 2	113	Peetre, Jaak			Cambridge, MA
.,,	110	Hampshire College	02	113	University of Lund	80	85	Thompson, John G.
		Amherst, MA			Lund, Sweden			University of Cambridge
83	100	Humphreys, James E.	76	79				Cambridge, UK
		University of Massachusetts		. ,	Polish Academy of	74	74	Timmesfeld, Frantz G.
		Amherst, MA			Sciences			University of Cologne
76	99	Kadison, Richard			Warsaw, Poland			Cologne, FRG
		Vincent University of Pennsylvania	71	96	Pletsch, Albrecht	88	102	Tits, Jacques
		Philadelphia, PA			University of Jena			College de France
96	124				Jena, GDR			Paris, France
		University of California	71	225	Reed, Michael Charles	83	130	Treves, Francoiz
		Berkeley, CA			Duke University			Rutgers University
68	74	Kervaire, Michel A.			Durham, NC			New Brunswick, NJ
		University of Geneva	74	151	Riesz, Friedrich	71	83	Triebel, Hans
		Geneva, Switzerland			University of Budapest			University of Jena
90	94	Knebusch, Manfred			Budapest, Hungary			Jena, GDR
		University of Regensburg Regensburg, FRG	95	111	Roseuthal, Haskell P.	80	82	Waldbausen, Friedbalm
82	121	*Kodaira, Kunihiko			University of Texas			University of Bielefeld
0.2		University of Tokyo			Austin, TX			Bielefeld, FRG
		Tokyo, Japan	70	109		80	108	
69	525				Lehigh University			University of Washington
		Nikolaevich			Bethlehem, PA			Seattle, WA
		USSR Academy of Sciences	83	182	Schoenberg, Isaac I.	75	87	
0:	4.0	Moscow, USSR			University of Wisconsin			University of California Berkeley, CA
96	169	Kostant, Bertram	22	6.	Madison, WI	100	jen	-
		Massachusetts Institute of Technology	72	86	Segal, Graeme Bryce Oxford University	100	189	Yosida, Kosaku Gakushuin University
		Cambridge, MA			Oxford, UK			Tokyo, Japan
		Camoringe, 1974			Catoro, Ca			- o-lot subati

Table 4: Institutional affiliations of the top 100 most-cited mathematicians of 1978 and 1979.

Institution	Number of Authors
University of Chicago, IL	9
Harvard University, Cambridge, MA	ь
Institute for Advanced Study, Princeton, NJ	6
University of California Berkeley (4) San Diego (1)	5
Yale University, New Haven, CT	4
Massachusetts Institute of Technology,	,
Cambridge, MA	3
University of Paris, France	3
VI, Pierre et Marie Curie (2) XI, Paris-Sud (1)	
California Institute of Technology, Pasadena	2
College de France, Paris	2
Hebrew University, Jerusalem, Israel	2
Kyoto University, Japan	2
New York University, New York	2
Oxford University, UK Princeton University, NJ	2 2
Rutgers University, New Brunswick, NJ	2
Stanford University, CA	2
Tulane University, New Orleans, LA	2
University of Gottingen, FRG	2
University of Washington, Seattle	2 1
Brandeis University, Waltham, MA Brown University, Providence, RI	1
Case Western Reserve University,	i
Cleveland, OH	
Centre National de la Recherche	1
Scientifique, Paris, France	1
Columbia University, New York, NY Duke University, Durham, NC	1
Ecole Polytechnique, Plaiseau, France	i
Hungarian Academy of Sciences.	i
Math Research Institute, Budapest	
Indiana University, Bloomington	1
Institut des Hautes Etudes Scientifiques, Bures-sur-Yvette, France	1
Johns Hopkins University, Baltimore, MD	1
Leningrad University, USSR	i
Mathematics Institute, USSR Academy of Sciences, Moscow	1
Moscow Control Problems Institute, USSR	1
Nihon University, Tokyo, Japan	1
Northwestern University, Evanston, IL State University of New York, Stony Brook	1
Tel Aviv University, Israel	i
University of Bonn, FRG	1
University of Cambridge, UK	1
University of Edinburgh, UK	1
University of Hamburg, FRG University of Liverpool, UK	1
University of London, UK	i
University of Lund, Sweden	i
University of Mainz, FRG	1
University of Manchester, UK	1
University of Michigan, Ann Arbor University of Minnesota, Minneapolis	1 1
University of Montpellier II, France	1
University of Nice, France	i
University of Oregon, Eugene	1
University of Oslo, Norway	1
University of Southern California, Los Angeles	1
University of Texas, Austin	1
University of Texas, Austin University of Tubingen, FRG University of Waterloo, Ontario, Canada	1
University of Waterloo, Ontario, Canada University of Wisconsin, Madison	1 1
Warsaw University, Poland	1

first two medals were awarded in 1936. A total of 24 mathematicians have won the medal since then. The 1982 Fields Medal winners will be announced later this year.

Table 4 lists the institutional affiliations of the top 100 most-cited pure mathematicians. Some of the mathematicians who reviewed the list observed that a few authors have retired or are deceased. Nevertheless, we feel it is important and useful to show their former institutional affiliations. Their work remains relevant to currently active mathematicians. Their institutions deserve to be acknowledged.

Interestingly, we cannot credit any institution with Nicolas Bourbaki's work—"he" is a secret group of mostly French mathematicians who publish under that collective pseudonym. Paul R. Halmos, Indiana University, Bloomington, claims that the membership of Bourbaki varies between ten and 20.9 At various times, several of the Bourbaki members were affiliated with the University of Chicago, Illinois; Northwestern University, Evanston, Illinois; Columbia University, New York; and the University of Nancy, France. André Weil is credited with being one of the founding fathers of the group, and Jean Dieudonné is described as "Bourbaki's chief scribe almost from the beginning" of the group's publications in the mid-1930s.9 Weil. Dieudonné, and Halmos appear on the list in Table 2.

The University of Chicago heads our list with nine most-cited mathematicians. The Institute for Advanced Study, Princeton, and Harvard University follow with six each. The University of California accounts for five, while Yale University has four. The University of Paris and Massachusetts Institute of Technology each have three. Twelve more institutions account for two each: California Institute of Technology; Collège de France, Paris; Hebrew University, Jerusalem; Kyoto University, Japan; New York University; Oxford University

ty; Princeton University; Rutgers University; Stanford University; Tulane University; University of Göttingen, Federal Republic of Germany; and University of Washington, Seattle.

Of the 58 institutions listed, just under half, 28, are located in the US, and 62 authors are affiliated with them. Ten mathematicians are affiliated with seven French institutions, not counting Bourbaki. Seven authors did their work at six UK institutions, and the Federal Republic of Germany accounts for five institutions and six authors. The USSR has three institutions and authors. Both Israel and Japan account for two institutions with three authors each. Canada, Hungary, Norway, Poland, and Sweden each have one institution and one author.

Table 5 lists the most-cited publication as a primary author for each of the 100 math authors. Also shown are the code numbers for ISI/CompuMath research fronts that include the publica-

tion as a core document. Seventy-nine are books. R. Courant and D. Hilbert's Methods of Mathematical Physics, the oldest book on the list, was published in 1924. The four newest books on the list were published in 1973, and were authored by H. Brézis, R.G. Douglas, Hormander, and J. Lindenstrauss and L. Tzafriri. In total, two books were published in the 1920s, five in the 1930s, two in the 1940s, ten in the 1950s, 47 in the 1960s, and 13 in the 1970s.

Of the 21 papers on the list, one was published in the 1930s, three in the 1950s, 11 in the 1960s, and six in the 1970s. The two most recent papers were published in 1977—Atiyah's "Instantons and algebraic geometry" and M. Sato's "Studies on holonomic quantum fields." The oldest, "Congruent graphs and the connectivity of graphs," by H. Whitney, was published in 1932.

As you can see, mathematicians tend to cite older literature. The so-called half-life of math research is much longer

Table 5: Most-cited publication as a primary author for each of the top 100 math authors. Publications which are in the core of an ISI/CompuMath. research front specialty are followed by the research front specialty number in bold.

Total SCI Citations 1978-1979 Bibliographic Data Adams J F. Stable homotopy and generalized homology 32 Chicago: University of Chicago Press, (1971) 1974, 305 p. 80-0039. 67 Agmon S. Lectures on elliptic boundary value problems. Princeton, NJ: Van Nostrand, 1965, 291 p. 24 Abliors L V. Lectures on quasiconformal mappings. Princeton, NJ: Van Nostrand, 1966, 146 p. 48 Alisen E.M. Compact convex sets and boundary integrals. New York: Springer-Verlag, 1971, 210 p. Artin M. On isolated rational singularities of surfaces. Amer. J. Math. 88:129-36, 1966. 80-0295. 19 Aschbacher M & Seltz G M. Involutions in Chevalley groups over fields of even order. Nagoya Math. J. 63:1-91, 1976. 80-0304. 48 Atiyah M F. Instantons and algebraic geometry. Commun. Math. Phys. 55:117-24, 1977. 80-0330. 15 Auslander M & Goldman O. The Brauer group of a commutative ring. Trans. Amer. Math. Soc. 97:367-409, 1960. 69 Bass H. Algebraic K-theory. New York: Springer-Verlag, (1968) 1973, 3 vols. 119 Bellman R E. Introduction to matrix analysis. New York: McGraw-Hill, (1960) 1970. 328 p. Berge C J. Graphes et hypergraphes. (Graphs and hypergraphs.) Paris: Dunod, (1960) 1970, 502 p. 165 100 Birkhoff G. Lattice theory Providence, RI: American Mathematical Society, (1940) 1973, 155 p. Borel A. Linear algebraic groups. New York: W.A. Benjamin, 1969. 398 p. 125 Bourbaki N. Algebre commutative (Commutative algebra.) Paris: Hermann, (1961) 1972, 625 p. Brauer R. Some applications of the theory of blocks of characters of finite groups. J. Algebra 1:152-67, 1964. 80-0858. Bredon G E. Introduction to compact transformation groups New York: Academic Press, 1972, 459 p. 55 Brezis H. Operateurs maximaux monotones et semi-groups de contractions dans les espaces de Hilbert. (Monotonic maximal operators and contraction semi-groups in Hilbert spaces.) Amsterdam: North Holland, 1973, 183 p. 12 Browder F E. Fixed point theory of multi-valued mappings in topological vector spaces. Math. Ann. 177:283-301, 1968, 19 Calderon A P & Zygmund A. On the existence of certain singular integrals. Acta Math. - Djursholm 88:85-139, 1952 Carlitz L. Arithmetic properties of generalized Bernoulli numbers J. Reine Angew. Math. 202:174-82, 1959.

Total SCI Citations 1978-1979	Bibliographic Data
104	Cartan H & Effenberg S. Homological algebra. Princeton, NJ: Princeton University Press, 1956. 390 p.
105	Clifford A H & Preston G B. The algebraic theory of semigroups.
3.5	Providence, RI: American Mathematical Society, (1961) 1977, 216 p. 80-1206.
35 3 98	Cohn P.M. Universal algebra. New York: Harper & Row, 1965. 333 p. Courant R & Hilbert D. Methoden der mathematischen physik. (Methods of mathematical
370	physics.) New York: Wiley. (1924) 1962. 2 vols.
92	Curtis C W & Reiner 1. Representation theory of finite groups and associative algebras.
	New York: Wiley, (1962) 1981, 685 p.
17	Deligne P, Griffiths P, Morgan J & Sullivan D. Real homotopy theory of Kahler manifolds.
74	Invent. Math. 29:245-74, 1975. Dieudonne I. Fondements de l'analyse moderne. (Foundations of modern analysis.)
	Paris: Gauthier-Villars, (1960) 1963. 374 p.
103	Dixmier I. Les algebres d'operateurs dans l'espace Hilbertien, algebres de Von Neumann.
	(Operator algebras in Hilbert space. Von Neumann algebras.)
30	Paris: Gauthier-Villars, (1957) 1969, 368 p.
29	Douglas R G. Banach algebra techniques in the theory of Toeplitz operators. Providence, RI: American Mathematical Society, 1973, 53 p.
469	Dunford N & Schwartz J T. Linear operators. New York: Wiley, (1958) 1971. 3 vols. 80-1539.
413	Erdelyi A, Magnus W, Oberhettinger F & Tricomi F G. Bateman manuscript project.
	(Higher transcendental functions.) New York: McGraw-Hill, 1953-55. 3 vols.
15	Erdos P, Ko C & Rado R. Intersection theorems for systems of finite sets.
21	Quart. J. Math. 12:313-20, 1961. Felt W & Thompson J G. Solvability of groups of odd order. Pac. J. Math. 13:775-1029, 1963.
164	Friedman A. Partial differential equations of parabolic type.
	Melbourne, FL: Krieger, (1964) 1976. 262 p.
127	Fuchs L. Infinite Abelian groups. New York: Academic Press, (1970) 1973. 2 vols. 80-1804.
198	Gelfand I M & Shilov G F. Generalized functions.
23	New York: Academic Press, (1964) 1967, 5 vols. 80-1867, Glauberman G. Central elements in core-free groups. J. Algebra 4:403-20, 1966.
38	Gokhberg I T & Krein M G. Vvedenie v teoriiu lineinykh nesamosopriazhennykh
	operatorov. (Introduction to the theory of linear nonselfadjoint operators.)
	Providence, RI: American Mathematical Society, (1965) 1969. 378 p.
145 21	Gorenstein D. Finite groups. New York: Chelsea, (1967) 1980. 527 p. Grauert H. Uber Modifikationen und exzeptionelle analytische Mengen. (Over-modification and
21	exceptional analytical numbers.) Math. Ann. 146:331-68, 1962.
59	Grothendleck A. Elements de geometrie algebrique. (Elements of geometric algebra.)
	New York: Springer-Verlag, (1960) 1971, 454 p.
45 82	Hale J K. Ordinary differential equations. Melbourne, FL: Krieger, (1969) 1980. 386 p.
92	Hall M. The theory of groups. New York: Chelsea, (1959) 1976. 434 p. Halmos P R, Measure theory. New York: Springer-Verlag, (1961) 1974. 305 p.
272	Harnry F. Graph theory. Reading, MA: Addison-Wesley, 1969. 274 p.
146	Hardy G H, Littlewood I E & Polya G. Inequalities.
	Cambridge, UK: Cambridge University Press, (1934) 1952. 324 p.
23	Harish-Chandra. Discrete series for semisimple Lie groups. II. Acta Math.—Djursholm 116:1-111, 1966. 80-1626.
100	Hartman P. Ordinary differential equations. New York: Wiley, 1964. 612 p.
26	Hartshorne R C. Residues and duality. New York: Springer-Verlag, 1966. 423 p.
17	Hasse H & Klobe W. Klassenzahl Abelscher Zahlkorper. (Number of classes of Abelian
139	number groups.) New York: F. Ungar, 1954. 212 p.
17	Helgason S. Differential geometry and symmetric spaces. New York: Academic Press, 1962, 486 p. Herstein I N. Topics in ring theory. Chicago: University of Chicago Press, (1965) 1969, 121 p.
140	Hewitt E & Ross K A. Abstract harmonic analysis. New York: Springer-Verlag. (1963) 1970. 2 vols.
137	HMe E. Functional analysis and semi-groups
	Providence, RI: American Mathematical Society, (1948) 1974. 528 p.
16 49	Hilton P J & Wylle S. Homology theory. Cambridge, UK: Cambridge University Press, (1960) 1961. 484 p. Hirzebruch F. Topological methods in algebraic geometry. New York: Springer-Verlag, (1956) 1978. 232 p
105	Hormander L. An introduction to complex analysis in several variables. New York: Elsevier, 1973. 213 p.
154	Huppert B. Endliche Gruppen. (Finite groups.) New York: Springer-Verlag, 1967. 796 p.
18	Iwasawa K. On Z ₁ extensions of algebraic number fields. Ann. Math. 98:246-326, 1973. 80-0943.
58	Jacobson N. Lie algebras. New York: Dover, (1962) 1979. 331 p.
44 48	Kaplansky I, Commutative rings. Chicago: University of Chicago Press, (1968) 1974. 129 p. Karlin S. Total positivity. Stanford, CA: Stanford University Press, 1968. 2 vols.
369	Kato T. Perturbation theory for linear operators. New York: Springer-Verlag, (1966) 1980, 619 p.
168	Kobayashi S & Nomizu K. Foundations of differential geometry. New York: Wiley, 1963. 329 p.
68	Krasnoselskii M A. Topological methods in the theory of nonlinear integral equations
177	New York: Macmillan, 1964, 395 p. 80-1816.
127 125	Kuratowski K., Topologie. (Topology.) New York: Academic Press, (1933) 1966. 2 vols. Ladyzhenskafa O A & Uraltseva N N. Lineinye i kvazilineinye uravneniia ellipticheskogo tipa.
	(Linear and quasilinear elliptic equations.) New York: Academic Press, (1964) 1968. 495 p.
71	Lang S. Algebra. Reading, MA: Addison-Wesley, 1965. 508 p.
71	Lax P D. Integrals of nonlinear equations of evolution and solitary waves.
	Commun. Pure Appl. Math. 21:467-90, 1968. 80-1843.

Total SC/ Citations	
1978-1979	Bibliographic Data
31	Lindenztrauss 1 & Trairiri L. Classical Banach spaces. New York: Springer-Verlag, 1973, 243 p.
115	Lions I L. Quelques methodes de resolution des problemes aux limits non lineaires. (Some
	methods for the resolution of problems with nonlinear limits.) Paris: Dunod, 1969, 554 p.
37	Lorentz G G. Approximation of functions. New York: Holt, Rinehart & Winston, 1966, 188 p.
31	Mackey G W. Induced representations of locally compact groups. I. Ann. Math. 55:101-39, 1952.
60	MacLane S. Homology. New York: Springer-Verlag, (1963) 1975, 422 p.
15	May J P. Simplicial objects in algebraic topology. New Haven, CT: Yale University Press, 1965. 182 p.
38	Milnor I W, Topology from the differentiable viewpoint.
	Charlottesville, VA: University Press of Virginia, 1965, 64 p.
32	Mumford D. Geometric invariant theory. New York: Springer-Verlag, 1965, 145 p.
57	Nagata M. Local rings. Melbourne, FL: Krieger, (1962) 1975, 248 p.
50	Polya G & Szego G. Aufgaben und Lehrsatze aus der Analysis. (Problems and theorems in analysis.) New York: Springer-Verlag, (1925) 1977, 2 vols.
27	Oullien D. Projective modules over polynomial rings. Invent. Math. 36:167-71, 1976.
159	Rockafellar R T. Convex analysis. Princeton, NJ: Princeton University Press, 1970, 451 p.
91	Rudin W, Real and complex analysis, New York: McGraw-Hill, (1966) 1973, 416 p.
71	Sakai S. C*-algebras and W*-algebras. New York: Springer-Verlag, 1971, 256 p.
15	Sato M, Miwa T & Jimbo M. Studies on holonomic quantum fields. I.
	Proc. Ipn. Acad. A 53:6-10, 1977. 80-2888.
74	Schaefer H. Topological vector spaces. New York: Springer-Verlag, (1966) 1971, 294 p.
91	Schwartz L. Theorie des distributions. (Theory of distributions.)
	Paris: Hermann, (1950-51) 1966. 2 vols. 80-2907; 80-2908.
50	Serre J P. Corps locaux. (Local groups.) Paris: Hermann, 1962, 243 p.
27	Shimura G. Introduction to the arithmetic theory of automorphic functions.
	Princeton, NJ: Princeton University Press, 1971, 267 p.
31	Slegel C L & Moser J K. Lectures on celestial mechanics. New York: Springer-Verlag, (1956) 1971, 290 p.
92	Spanler E.H. Algebraic topology, New York: McGraw-Hill, 1966, 528 p.
144	Steln E M. Singular integrals and differentiability properties of functions
	Princeton, NJ: Princeton University Press, (1970) 1971. 287 p.
14 67	Swan R G. Periodic resolutions for finite groups. Ann. Math. 72:267-91, 1960. 80-1793. The theory of functions. London: Oxford University Press, (1932) 1952. 454 p.
18	Tutte W. T. Connectivity in graphs. Toronto: University of Toronto Press, 1966, 145 p.
33	Wall C T C. Surgery on compact manifolds. New York: Academic Press, 1900, 1971, 280 p.
29	Well A. Basic number theory. New York: Springer-Verlag, (1967) 1975, 325 p.
75	Weyl H. The classical groups. Princeton, NJ: Princeton University Press, (1939) 1946, 320 p.
14	Whitney H. Congruent graphs and the connectivity of graphs. Amer. J. Math. 54:150-68, 1932.
120	Zariski O & Samuel P. Commutative algebra. New York: Springer-Verlag, (1958) 1976. 2 vols. 80-0547.
243	Zygmund A. Trigonometrical series. Cambridge, UK: Cambridge University Press, (1935) 1977, 331 p.

than other fields. It is not unusual for important mathematical works to be used decades after publication. That's one reason why our ISI/CompuMath files will eventually cover at least 30 years of literature. Several mathematicians noted that the significance of many mathematical discoveries is often appreciated only after a long time. Of course, this would not affect the validity of our study—its purpose is to identify the mathematicians most cited in 1978 and 1979, regardless of when their works were published. But it would be interesting to note patterns of citation to more contemporary mathematicians. For example, we could study the most-cited math authors who have published between 1965 and 1980, much as we did in the life and physical sciences.1

The 100 publications in Table 5 were written by only 132 authors. More than

three quarters (61) of the 79 books listed have one author—this includes the group of authors publishing under Bourbaki. Sixteen books have two authors, one has three, and one has four. Fourteen of the 21 papers have one author. Four papers have two authors, two have three, and one has four.

Table 6 lists the names of the ISI/CompuMath research fronts that include one or more of the most-cited works in Table 5 as a core document. The research front names are created by examining the most-used words or phrases in the titles of articles citing the core publications. Also shown are the mathematicians in this study whose most-cited publication appears in the research front.

The data in these tables illustrate how important it is to do these citation analyses on a field-by-field basis. The

Table 6: Titles of ISI/CompuMath'* research fronts that include most-cited works by the top 100 math authors among their core documents. The names of the mathematicians in this study whose most-cited publication is included in the research front are shown in parentheses.

Research Front	
Number	Research Front Name
80-0039	Adams-Novikov spectral sequence, Brown-Peterson homology, Morava K-theory, and complex cobordism (Adams J F)
80-0295	Rational singularities, elliptic singularities, and normal singularities of surfaces (Artin M)
80-0304	Standard components and standard subgroups of finite simple groups (Aschbacher M)
80-0330	Yang-Mills gauge theories, Euclidean self-dual solutions, and instantons (Atiyah M F)
80-0547	Ultraproducts, power series equations, and curves with large tangent space (Zariski O)
80-0858	Blocks of characters and the structure of finite groups (Brauer R)
80-0943	P-adic L-functions, cyclotomic fields, and Iwasawa invariants (Iwasawa K)
80-1206	Semigroups: structure theorems, inverse semigroups, divisibility, lattice of ideals; representations, embedding theorems, and free semigroups (Clifford A H)
80-1539	Controllability and observability for distributed-parameter systems in Banach spaces (Dunford N)
80-1626	Representations, characters, and discrete series for semisimple Lie groups (Harish-Chandra)
80-1793	Finite groups with trivial class groups, a normal integral basis theorem, periodic projective resolutions, and locally free class groups of groups of prime power order (Swan R G)
80-1804	Injectivity, projectivity, torsion, and other properties of Abelian groups (Fuchs L)
80-1816	Spectral theory for nonlinear operators in normed spaces (Krasnoselskii M A)
80-1843	Evolution equations, Backlund transformations for a higher order Korteweg-Devries equation, and nonlinear partial differential equations solvable by inverse-scattering transforms (Lax P D)
80-1867	Localization in quantum field theory: Fourier hyperfunctions, the Bogolyubov axiomatic approach, and a relativistic invariant formulation of causality (Gelfand I M)
80-2888	Studies on holonomic quantum fields (Sato M)
80-2907	Cauchy problems, eigenspaces, and general solutions of differential equations (Schwartz L)
80-2908	Distribution theory, generalized functions, differential operators, and compact groups (Schwartz L)

most surprising result to one who is not a mathematician is the dominance of books. This is a result I might have expected in the humanities or social sciences, or even in engineering. However, the results were not so surprising to the many mathematicians who examined the list. Several commented that they would have preferred that we limit the list to journal articles. Such an approach might

have given a different perspective on current mathematical research. This will be easy to do in a future study based on even more up-to-date information.

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 Essays of an information scientist. Philadelphia: ISI Press, 1980. Vol. 3. p. 326-36.
 (Reprinted from: Current Contents (49):5-15, 5 December 1977.)
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- Mostow G D. The Fields Medals (I): relating the continuous and the discrete. Science 202:297-8, 1978.
- 9. Halmos P R. "Nicolas Bourbaki." Sci. Amer. 196:88-91; 93-4; 96; 99, 1957.